



1. The subclass $\mathcal{S}_{\Sigma}^{h,p}$

In this section, we introduce and investigate the general subclass $\mathcal{S}_{\Sigma}^{h,p}$.

Definition 1..1. Let the functions $h, p : \mathbb{U} \rightarrow \mathbb{C}$ be so constrained that

$$\min\{\Re(h(z)), \Re(p(z))\} > 0 \quad z \in \mathbb{U} \quad \text{and} \quad h(0) = p(0) = 1$$

Also let the function f , defined by (??), be in the analytic function class \mathcal{A} . we say that

$$f \in \mathcal{S}_{\Sigma}^{h,p}(k, \lambda) \quad , \quad (k \in \mathbb{N}_0, 0 \leq \lambda < 1)$$

if the following conditions are satisfied:

$$f \in \Sigma \quad \text{and} \quad \frac{\mathcal{D}^{k+1}f(z)}{(1-\lambda)\mathcal{D}^k f(z) + \lambda\mathcal{D}^{k+1}f(z)} \in h(\mathbb{U}) \quad (z \in \mathbb{U}) \quad (1..1)$$

and

$$\frac{\mathcal{D}^{k+1}g(w)}{(1-\lambda)\mathcal{D}^k g(w) + \lambda\mathcal{D}^{k+1}g(w)} \in p(\mathbb{U}) \quad (w \in \mathbb{U}). \quad (1..2)$$

where the function $g(w)$ is given by (??).